## Game Theory with Application in Economics and Finance Magistère BFA 2 - Fall 2015

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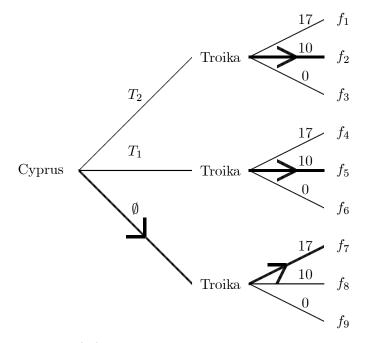
Solution Exercise Chap.2

## Cyprus: Taxation of bank deposits to avoid a euro exit

1. From  $(I_4)\&(I_5)$  the three possible Cyprus actions are: not to implement any tax, denoted by  $\emptyset$ ; to adopt the tax  $T_1$ ; or to adopt the tax  $T_2$ .

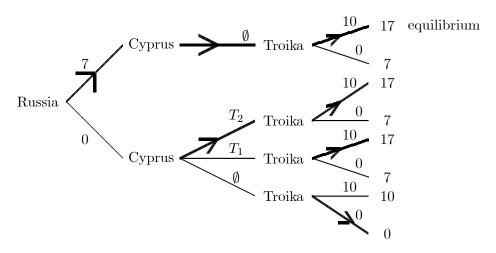
From  $(I_6)$  the three possible troika's (EU, ECB and IMF) actions are: to not take part in the rescue plan, denoted by 0; to lend 10 billion euros, denoted by 10; or to lend 17 billion euros, denoted by 17.

2. The sequential form game played by Cyprus and the troika where Cyprus moves first depicts as (ignore the array for the moment):

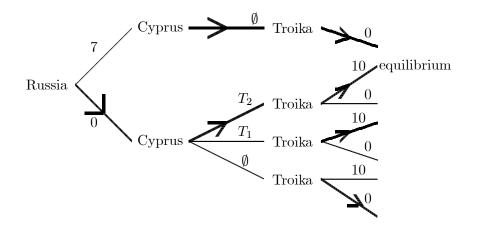


3. From  $(I_3)$  Cyprus rescue requires a help estimated at 17 billion euros. The leaves corresponding to a rescue are:  $\{f_1, f_2, f_4, f_5, f_7\}$ .

- 4. From  $(I_1)\&(I_2)\&(I_3)$  the troika prefers a Cyprus rescue, but wants to be involved as less as possible. Therefore, troika's preferred leaves when Cyprus plays:  $T_2$  is  $f_2$ ;  $T_1$  is  $f_5$ ; and  $\emptyset$  is  $f_7$ .
- 5. From  $(I_5)$ , Cyprus prefers  $f_2$  to  $f_5$ . From  $(I_2)$  Cyprus prefers  $f_7$  to  $f_2$  and  $f_5$ . Finally, among the three preceding leaves, Cyprus prefers  $f_7$ .
- 6. The backward induction outcome is  $f_7$ : the troika is the only player involved in the Cyprus rescue.
- 7. From  $(I_8)$  there are only two possible troika's actions: to not take part in the rescue plan, denoted by 0; to lend 10 billion euros, denoted by 10. From  $(I_7)$  Russia's actions are: to not take part in the rescue plan, denoted by 0; to lend 7 billion euros, denoted by 7.
- 8. The sequential form game played by Russia, Cyprus and the troika where Russia moves first and Cyprus moves second depicts as (ignore the array for the moment):



- 9. The backward induction outcome consists in Russia lending 7 billion euros and the troika lending 10 billion euros.
- 10. From  $(I_2)$  the troika prefers this equilibrium to the one of question **6** because in both cases Cyprus is rescued but the troika lends a lower amount in the second case.
- 11. From  $(I_9)$  the troika will provide assistance only if Russia does not participate. The new game tree in the sequential order of question **8** depict as (ignore the array for the moment):



- 12. The backward induction outcome consists in Cyprus implementing the tax  $T_2$  to raise 7 billion euros and the troika lending 10 billion euros.
- 13. From  $(I_2)$  the troika prefers this equilibrium to the one of question **6** because the rescue is performed at a lower lending amount from the troika (10 rather than 17 billion euros). From  $(I_9)$  the troika also prefers this equilibrium to the one of question **10** because now there is no more Russia participation.
- 14. By announcing a bailout reduction from 17 to 10 billion euros  $(I_8)$  and by providing Cyprus government with incentives to renounce to any Russian assistance  $(I_9)$ , the troika succeeds to implement his first-best equilibrium outcome.